Tim Fernando and Carl Vogel (Dublin, Ireland)

Prague, 19 February 2019

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HANS KAMP: discourse time (from events)

when we interpret a piece of discourse — or a single sentence in the context in which it is being used — we build something like a model of the episode or situation described; and an important part of that model are its event structure, and the time structure that can be derived from that event structure

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ISO-TimeML (PUSTEJOVSKY, LEE, BUNT, ...): TLINK tags

 $\S 1$ Allen interval relations

- §1 Allen interval relations
- $\S 2$ Probabilities over n ordered points

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- $\S 3$ Probabilities over n interval names

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- §4 Conclusion

- §1 Allen interval relations
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Allen relations

$$a \approx (I(a), r(a)] \approx \{x \mid I(a) < x \leq r(a)\}$$

$$ama' : I(a) < r(a) = I(a') < r(a')$$

Allen relations as strings (SCHWER, DURAND)

$$a \approx (I(a), r(a)] \approx \{x \mid I(a) < x \leq r(a)\}$$

$$\mathsf{am} \mathsf{a}' : \mathsf{I}(\mathsf{a}) < \mathsf{r}(\mathsf{a}) = \mathsf{I}(\mathsf{a}') < \mathsf{r}(\mathsf{a}')$$
 $\boxed{\mathsf{I}(\mathsf{a}) \mid \mathsf{r}(\mathsf{a}), \mathsf{I}(\mathsf{a}') \mid \mathsf{r}(\mathsf{a}')}$

$$aba' : I(a) < r(a) < I(a') < r(a')$$
 $I(a) | r(a) | I(a') | r(a') |$

Allen relations as strings (SCHWER, DURAND)

$$a \approx (I(a), r(a)] \approx \{x \mid I(a) < x \leq r(a)\}$$

$$ama' : I(a) < r(a) = I(a') < r(a') \qquad \boxed{I(a) \mid r(a), I(a') \mid r(a')}$$
$$\mathfrak{s}_{m}(a, a') := \boxed{a \mid a, a' \mid a'}$$

$$aba'$$
: $I(a) < r(a) < I(a') < r(a')$ $I(a) | r(a) | I(a') | r(a')$

Allen relations as strings (SCHWER, DURAND)

$$a \approx (I(a), r(a)] \approx \{x \mid I(a) < x \leq r(a)\}$$

$$ama' : l(a) < r(a) = l(a') < r(a')$$

$$\mathfrak{s}_{m}(a, a') := \boxed{a \mid a, a' \mid a'}$$

$$aba'$$
: $I(a) < r(a) < I(a') < r(a')$
$$\boxed{I(a) \mid r(a) \mid I(a') \mid r(a')}$$

$$\mathfrak{s}_{R^{-1}}(a,a')=\mathfrak{s}_R(a',a)$$

$$t(R_1,R_2):=\{R\in\mathcal{AR}\mid \text{for some order with intervals }a,a',a'',\ aR_1a',\ a'R_2a'' \text{ and }aRa''\}$$
 e.g. $t(b,b)=\{b\}$ $t(o,d)=\{d,o,s\}$ $t(b,bi)=\mathcal{AR}$

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 $R' \in AR$

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 $R' \in AR$

$$t(R_1,R_2) := \{R \in \mathcal{AR} \mid \text{ for some order with intervals } a,a',a'', \\ aR_1a',\ a'R_2a'' \text{ and } aRa''\}$$
 e.g.
$$t(\mathsf{b},\mathsf{b}) = \{\mathsf{b}\} \qquad t(\mathsf{o},\mathsf{d}) = \{\mathsf{d},\mathsf{o},\mathsf{s}\} \qquad t(\mathsf{b},\mathsf{bi}) = \mathcal{AR}$$

$$\#(R) := \sum_{R' \in \mathcal{AR}} \mathsf{card}(t(R,R')) = \sum_{R' \in \mathcal{AR}} \mathsf{card}(t(R',R))$$

$$= \begin{cases} 41 & \text{if length}(\mathfrak{s}_R) = 4 \\ 25 & \text{if length}(\mathfrak{s}_R) = 3 \end{cases} \pmod{\mathsf{medium}} \mathsf{m,s,f,mi,si,fi}$$

$$13 & \text{if length}(\mathfrak{s}_R) = 2 \qquad (\mathsf{short: e})$$

- §1 Allen interval relations
- $\S 2$ Probabilities over n ordered points
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```
[n] := \{1, 2, \dots, n\}
\Omega_n := \{f : \{x, y, x', y'\} \rightarrow [n] \mid f(x) < f(y) \text{ and } f(x') < f(y')\}
```

$$\begin{aligned} [n] &:= \{1, 2, \dots, n\} \\ \Omega_n &:= \{f \colon \{x, y, x', y'\} \to [n] \mid f(x) < f(y) \text{ and } f(x') < f(y')\} \\ & f \text{ satisfies } R \iff (f(x), f(y)] \ R \ (f(x'), f(y')] \\ & p_n(R) &= \frac{\mathsf{card}(\{f \in \Omega_n \mid f \text{ satisfies } R\})}{\mathsf{card}(\Omega_n)}. \end{aligned}$$

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$$\Omega_n := \{f : \{x, y, x', y'\} \rightarrow [n] \mid f(x) < f(y) \text{ and } f(x') < f(y')\}$$

$$f \text{ satisfies } R \iff (f(x), f(y)] R (f(x'), f(y')]$$

$$p_n(R) = \frac{\operatorname{card}(\{f \in \Omega_n \mid f \text{ satisfies } R\})}{\operatorname{card}(\Omega_n)}.$$
where for $n \ge 4$, $\operatorname{card}(\{f \in \Omega_n \mid f \text{ satisfies } R\})$ is
$$\binom{n}{2} = \frac{n(n-1)}{2} \quad \text{if } R \text{ is e}$$

$$\binom{n}{3} = \binom{n}{3} \frac{n-2}{3} \quad \text{if } R \text{ is medium}$$

$$\binom{n}{4} = \binom{n}{3} \frac{n-3}{4} \quad \text{if } R \text{ is long}$$

Probabilities calculated

For
$$n \geq 4$$
 and $R, R' \in \mathcal{AR}$,

$$p_n(R) = p_n(R')$$
 if $length(\mathfrak{s}_R) = length(\mathfrak{s}_{R'})$

Probabilities calculated

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and

$$\operatorname{card}(\Omega_n) = \binom{n}{2} \cdot \binom{n}{2}$$

whence

$$p_n(e) = \frac{2}{n(n-1)}$$

$$p_n(R) = \frac{2(n-2)}{3n(n-1)} \quad \text{for medium } R$$

$$p_n(R) = \frac{(n-3)(n-2)}{6n(n-1)} \quad \text{for long } R$$

Some probabilities

$$\lim_{n\to\infty} p_n(R) = \begin{cases} 0 & \text{if } R \text{ is short or medium} \\ 1/6 & \text{otherwise} \end{cases}$$

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n	$p_n(e)$	$p_n(m)$	$p_n(b)$
4	1/6	1/9	1/36
5	1/10	1/10	1/20
6	1/15	4/45	1/15
8	1/28	1/14	5/56

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$$\mathcal{L}_n := \{ s \in (2^{[n]} - \{\square\})^+ \mid \text{each } i \in [n] \text{ occurs exactly twice in } s \}$$

$$\mathcal{L}_2 = \{ \mathfrak{s}_R(1,2) \mid R \in \mathcal{AR} \}$$

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$$\pi_{A}(\alpha_{1}\cdots\alpha_{n}) := (\alpha_{1}\cap A)\cdots(\alpha_{n}\cap A) \text{ and then delete any } \square$$

$$\pi_{\{2,3\}}(\boxed{1,2,4 \ | \ 1 \ | \ 2,3 \ | \ 3 \ | \ 4}) = \boxed{2 \ | \ 2,3 \ | \ 3}$$

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$$i$$
 occurs exactly twice in $s \iff \pi_{\{i\}}(s) = \boxed{i \mid i}$
$$s \models iRi' \iff \pi_{\{i,i'\}} = \mathfrak{s}_R(i,i')$$

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$$i$$
 occurs exactly twice in $s \iff \pi_{\{i\}}(s) = \lfloor i \rfloor i \rfloor$
$$s \models iRi' \iff \pi_{\{i,i'\}} = \mathfrak{s}_R(i,i')$$

$$f:[n]\times[n] o \mathcal{AR}$$
 is consistent if for some $s\in\mathcal{L}_n$,

$$(\forall i \in [n])(\forall i' \in [n]) \ \pi_{\{i,i'\}}(s) = \mathfrak{s}_{f(i,i')}(i,i')$$

Fact.

(i) For all $s \in \mathcal{L}_n$ and $(i, i') \in [n] \times [n]$, there is a unique $R \in \mathcal{AR}$ s.t. $\pi_{\{i, i'\}}(s) = \mathfrak{s}_R(i, i')$.

Fact.

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- (ii) The map $s \mapsto \omega_s$ is a bijection from \mathcal{L}_n onto the set of consistent labellings from $[n] \times [n]$ to \mathcal{AR} , where $\omega_s : [n] \times [n] \to \mathcal{AR}$ sends (i, i') to the unique $R \in \mathcal{AR}$ s.t. $\pi_{\{i, i'\}}(s) = \mathfrak{s}_R(i, i')$.

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$$\mathcal{L}_n(R) := \{ s \in \mathcal{L}_n \mid \pi_{\{1,2\}}(s) = \mathfrak{s}_R(1,2) \}$$

$$p_n(R) := \frac{\operatorname{card}(\mathcal{L}_n(R))}{\operatorname{card}(\mathcal{L}_n)}$$

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Calculate $card(\mathcal{L}_n(R))$ and $card(\mathcal{L}_n)$ through superposition

Superposition

&(
$$[i \mid i], [i' \mid i'], s$$
) \iff $s \in \{\mathfrak{s}_R(i,i') \mid R \in \mathcal{AR}\}.$

(i0)
$$\frac{\&(s,s',s'')}{\&(s\alpha,s'\alpha',s''(\alpha\cup\alpha'))}$$

(i2) $\frac{\&(s,s',s'')}{\&(s\alpha,s',s''\alpha)}$
(i3) $\frac{\&(s,s',s'')}{\&(s,s'\alpha',s''\alpha')}$

Superposition

&(
$$[i]i$$
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$$\frac{\&(s,s',s'')}{\&(s\alpha,s',s''\alpha')}$$
(i3)
$$\frac{\&(s,s',s'')}{\&(s,s'\alpha',s''\alpha')}$$

$$\stackrel{\text{(i0)}}{\leadsto} (\epsilon, \epsilon, \epsilon) \stackrel{\text{(i2)}}{\leadsto} (\boxed{i}, \epsilon, \boxed{l}) \stackrel{\text{(i1)}}{\leadsto} (\boxed{i} \boxed{i}, \boxed{i'}, \boxed{i} \boxed{i, i'})$$

$$\stackrel{\text{(i3)}}{\leadsto} (\boxed{i} \boxed{i}, \boxed{i'} \boxed{i'}, \boxed{i} \boxed{i, i'} \boxed{i'})$$

Superposition

&
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(i3) $\frac{\&(s,s',s'')}{\&(s,s'\alpha',s''\alpha')}$

$$(\epsilon, \epsilon, \epsilon) \stackrel{(i2)}{\leadsto} (\bar{i}, \epsilon, \bar{I}) \stackrel{(i1)}{\leadsto} (\bar{i}, \bar{i}', \bar{i}', \bar{i}', i')$$

$$\stackrel{(i3)}{\leadsto} (\bar{i}, \bar{i}', \bar{i}', \bar{i}', \bar{i}', i')$$

$$L\&L' := \{s'' \mid (\exists s \in L)(\exists s' \in L') \&(s, s', s'')\}$$

A commutative monoid

$$egin{array}{lll} \mathcal{L}_1 &= \boxed{1} \boxed{1} \\ \mathcal{L}_{n+1} &= \mathcal{L}_n \ \& \ \boxed{n+1} \ \boxed{n+1} & ext{for } n \geq 1 \end{array}$$

A commutative monoid

$$\mathcal{L}_1 = \boxed{1} \boxed{1}$$
 $\mathcal{L}_{n+1} = \mathcal{L}_n \& \boxed{n+1 \mid n+1}$ for $n \ge 1$

$$\mathcal{L}_2(R) = \mathfrak{s}_R(1,2)$$
 $\mathcal{L}_{n+1}(R) = \mathcal{L}_n(R) \& \boxed{n+1 \mid n+1}$ for $n \ge 2$

A commutative monoid

$$\mathcal{L}_1 = \boxed{1 \ 1}$$
 $\mathcal{L}_{n+1} = \mathcal{L}_n \& \boxed{n+1 \ n+1}$ for $n \geq 1$

$$\mathcal{L}_2(R) = \mathfrak{s}_R(1,2)$$
 $\mathcal{L}_{n+1}(R) = \mathcal{L}_n(R) \& \boxed{n+1 \mid n+1}$ for $n \ge 2$

Given a string s of length k > 1, the set $s \& \lceil n \rceil n \rceil$ consists of

- $\binom{k}{2}$ strings of length k,
- k(k+1) strings of length k+1, and
- $\binom{k+1}{2} + k + 1$ strings of length k+2

Cardinalities of $\mathcal{L}_n(R)$ and \mathcal{L}_n

$$\begin{array}{rcl} c_n(R;k) &:= \operatorname{card}(\{s \in \mathcal{L}_n(R) \mid \operatorname{length}(s) = k\}) \\ c_2(R;k) &= \left\{ \begin{array}{ll} 1 & \text{if length}(\mathfrak{s}_R) = k \\ 0 & \text{otherwise} \end{array} \right. \\ c_{n+1}(R;k) &= \frac{k(k-1)}{2}(c_n(R;k) + 2c_n(R;k-1) + c_n(R;k-2)) \end{array}$$

Cardinalities of $\mathcal{L}_n(R)$ and \mathcal{L}_n

$$c_n(R;k) := \operatorname{card}(\{s \in \mathcal{L}_n(R) \mid \operatorname{length}(s) = k\})$$

$$c_2(R;k) = \begin{cases} 1 & \text{if length}(\mathfrak{s}_R) = k \\ 0 & \text{otherwise} \end{cases}$$

$$c_{n+1}(R;k) = \frac{k(k-1)}{2}(c_n(R;k) + 2c_n(R;k-1) + c_n(R;k-2))$$

$$\operatorname{card}(\mathcal{L}_n(e)) = \sum_{k=2}^{2n-2} c_n(e;k)$$

$$\operatorname{card}(\mathcal{L}_n(R)) = \sum_{k=3}^{2n-1} c_n(R;k) \quad \text{for medium } R$$

$$\operatorname{card}(\mathcal{L}_n(R)) = \sum_{k=3}^{2n} c_n(R;k) \quad \text{for long } R$$

 $\operatorname{card}(\mathcal{L}_n) = \operatorname{card}(\mathcal{L}_n(e)) + 6(\operatorname{card}(\mathcal{L}_n(m)) + \operatorname{card}(\mathcal{L}_n(b)))$

$\operatorname{card}(\mathcal{L}_n(R))/\operatorname{card}(\mathcal{L}_n)$ for some n

n	$p_n(e)$	$p_n(m)$	$p_n(b)$	$1 - 6p_n(b)$
2	1/13	1/13	1/13	$7/13 \approx 0.5384615$
3	0.03178484	1 0.061124694	0.100244499	0.398533007
10	0.00252776	1 0.021841026	0.144404347	0.133573915
100	0.00002378	2 0.002283051	0.164379652	0.013722086
500	0.00000095	9 0.000460405	0.166206102	0.002763387
100	0 0.00000024	0 0.000230840	0.166435786	0.001385281
150	0.00000010	7 0.000153893	0.166512755	0.000923468

$\operatorname{card}(\mathcal{L}_n(R))/\operatorname{card}(\mathcal{L}_n)$ for some n

n	$p_n(e)$	$p_n(m)$	$p_n(b)$	$1 - 6p_n(b)$
2	1/13	1/13	1/13	$7/13 \approx 0.53846153$
3	0.031784841	0.061124694	0.100244499	0.398533007
10	0.002527761	0.021841026	0.144404347	0.133573915
100	0.000023782	0.002283051	0.164379652	0.013722086
500	0.000000959	0.000460405	0.166206102	0.002763387
1000	0.000000240	0.000230840	0.166435786	0.001385281
1500	0.00000107	0.000153893	0.166512755	0.000923468

$$p_2(R) = rac{1}{13}$$
 uniform distribution $p_3(R) = rac{\#(R)}{\sum_{R' \in \mathcal{AR}} \#(R')}$ transitivity table

PLAN

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HANS KAMP: discourse time (from events)

when we interpret a piece of discourse — or a single sentence in the context in which it is being used — we build something like a model of the episode or situation described; and an important part of that model are its event structure, and the time structure that can be derived from that event structure

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(MLN)
$$p(x) = \frac{1}{Z} exp(\sum_{\varphi \in I} w_{\varphi} n_{\varphi}(x))$$

- finite set I of f-o formulas arphi and weights $w_{arphi} \in \mathbb{R}$
 - $n_{\varphi}(x)$ is the number of x-groundings satisfying φ uniform if $\{\varphi \in I \mid w_{\varphi} \neq 0\} = \emptyset$ (data-free)

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when we interpret a piece of discourse — or a single sentence in the context in which it is being used — we build something like a model of the episode or situation described; and an important part of that model are its event structure, and the time structure that can be derived from that event structure by means of Russell's construction.

(MLN)
$$p(x) = \frac{1}{Z} exp(\sum_{\varphi \in I} w_{\varphi} n_{\varphi}(x))$$

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Stretches of time

 $Russell-instant = maximal \ subset \ of \ overlapping \ events$

$$a, a' + a a' + a' a$$



Stretches of time

Russell-instant = maximal subset of overlapping events

$$\begin{bmatrix} a, a' \end{bmatrix} + \begin{bmatrix} a & a' \end{bmatrix} + \begin{bmatrix} a' & a \end{bmatrix}$$

+ pre, post for all Allen relations on a, a' — e.g.,

Stretches of time

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+ pre, post for all Allen relations on a, a' — e.g.,

$$\underbrace{\left(\begin{array}{c} \text{interior} \\ I \end{array}\right]}_{r}$$

Stretches of time vs moments of change

Russell-instant = maximal subset of overlapping events

$$\begin{bmatrix} a, a' \end{bmatrix} + \begin{bmatrix} a & a' \end{bmatrix} + \begin{bmatrix} a' & a \end{bmatrix}$$

+ pre, post for all Allen relations on a, a' — e.g.,

- analyze in Monadic Second-Order Logic (MSO) over strings

Leibniz' law (identity of indiscernibles)

$$x \neq y \supset (\exists P) \neg (P(x) \equiv P(y))$$
 (LL)

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- take P from a finite set A

$$x \not\equiv_A y := \bigvee_{a \in A} \neg (P_a(x) \equiv P_a(y))$$
$$\equiv \bigvee_{a \in A} (\neg P_a(x) \land P_a(y)) \lor (P_a(x) \land \neg P_a(y))$$

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- replace \neq by adjacency S

$$xSy \supset x \not\equiv_A y$$
 (LL_{S,A})

Leibniz' law (identity of indiscernibles) & projections

$$x \neq y \supset (\exists P) \neg (P(x) \equiv P(y))$$
 (LL)

- take P from a finite set A

- replace \neq by adjacency S "time steps_S only with change_A"

$$x S y \supset x \not\equiv_{A} y \tag{LL}_{S,A}$$

Thank You